### Problem set 2 - Answers

September 29, 2025

I really need to still look over these and compare them to the way the problems are stated.

#### 1. Time dilation:

$$\gamma = 1/\sqrt{1 - v^2/c^2} = 1/\sqrt{1 - 0.6^2} \approx 1.25$$

Earth time =  $\gamma \times$  Spaceship time

Earth time = 1.25 \* 2 hours = 2.5 hours

#### 2. The frames coincide at the first event.

So the first event is at t = 0, x = 0 in both frames.

$$\gamma = \frac{5}{3}$$
 or about 1.67

Lorentz transform the 2nd event, and it occurs at

$$t = 8.33$$
,  $x = 6.67$  in the other frame.

So the spatial separation is about  $6.67\mu s$  or around 2,000 meters.

Or you could dilate the time ...

Then 8.33 seconds passes in the primed frame.

And the distance traveled is  $x=vt \approx (8.33)(.8)$  giving the same answer.

## 3. Length contraction:

$$L' = L/\gamma$$
$$\gamma = 1/\sqrt{1 - 0.5^2} \approx 1.15$$

$$L' = 1m/1.15 \approx 0.87m$$

## 4. Time dilation for muon decay:

$$\gamma \approx 7.09 \text{ (for v} = 0.99c)$$

Proper lifetime = 2.2 
$$\mu s$$

Dilated lifetime = 
$$7.09 \times 2.2 \mu s \approx 15.6 \mu s$$

Distance = 
$$0.99c \times 15.6 \mu s \approx 4.63 km$$

# 5. Time dilation for light clock:

Proper time between bounces = 2 seconds

Dilated time = 
$$\gamma \times 2$$
 seconds

$$\gamma \approx 1.25(v = 0.6c)$$

Dilated time = 
$$1.25 \times 2 = 2.5$$
 seconds

Number of bounces in 10 seconds = 10 / 2.5 = 4 bounces

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## 6. Time dilation to cause 2-second delay:

This is a Lorentz transform problem.

The correct answer is 
$$\frac{2}{\sqrt{13}}$$
.

#### 7. Length contraction:

$$L' = L/\gamma$$
$$\gamma \approx 1.67(v = 0.8c)$$
$$L' = 100m/1.67 \approx 59.9m$$

#### 8. Relativistic velocity addition:

$$\mathbf{v} = (v_1 + v_2)/(1 + v_1 v_2)$$
  
 $\mathbf{v} = (0.75 + 0.75)/(1 + 0.75 \times 0.75) \approx 0.96c$